

## EFFECT OF INTERACTION BETWEEN INERTIAL FORCE AND NORMAL / REVERSE FAULT DISPLACEMENT ON PC RAHMEN BRIDGE

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### ABSTRACT

*This paper conducts the analytical investigation of the differences between a bridge response under only inertial force and, that under both fault displacement and inertial force. These analyses were conducted by using static analyses and dynamic analyses considering relative displacements under normal and reverse slip with various fault displacements. According to the analytical results, it can be concluded that the effect of inertial force tends to be less, when the fault displacement becomes large.*

**KEYWORDS:** Normal Fault, Reverse Fault, Inertial Force, EPS Method & PC Rahmen Bridge

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### 1. INTRODUCTION

The seismic response of bridges during earthquakes is caused by its inertial force. Practically speaking, many earthquakes brought about severe damage to bridges and this damage was wreaked by large inertial forces. As bridges are top-heavy structures, earthquakes affect bridge structures especially.

In general, a bridge structure is supported by more than one support point. When these support points vibrate in the same way, we can consider that the bridge is affected by only inertial force. However, when the support points oscillate in different ways, we should consider the damage caused by the relative displacement between the support points.

Especially, fault movement taking place on the ground-surface, large relative displacement will generate and it will affect the damage of the bridge. As a matter of course, the relative displacement depends on the magnitude of the fault. It also can be seen that the degree of bridge damage, considering both effect of its inertial force and relative displacement is greater than that only considering effect of its inertial force.

However, the effect of the fault displacement to bridges damage isn't clarified easily. Therefore, it is quite important for seismic design to have the information of the dominant factor of bridge damage.

Therefore, the differences between 1- the bridge response, only considering inertial force and, 2- the bridge response considering both fault displacement and inertial force are taken in this study. These analyses were conducted by using static analyses and dynamic analyses considering relative displacements under normal and reverse slip, with various fault displacements.

### 2. TARGET BRIDGE AND ITS FE MODEL

To evaluate the effect of fault displacement and the coupling effect of relative displacement and inertial force, a PC rahmen bridge shown in Figure 1 is analyzed. The cross section of the mainspan and the side spans are



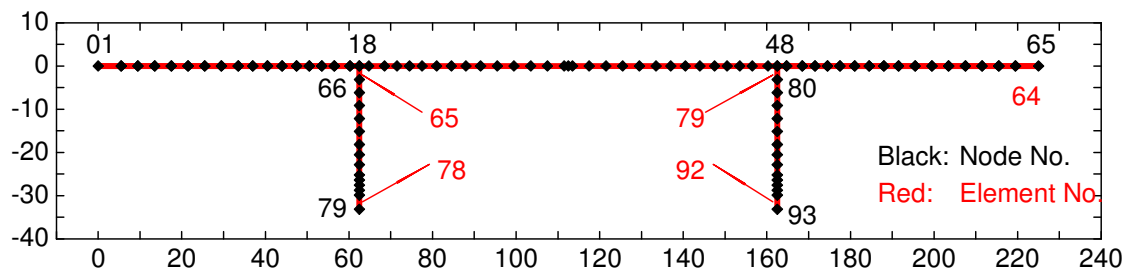


Figure 4: Beam Element Model

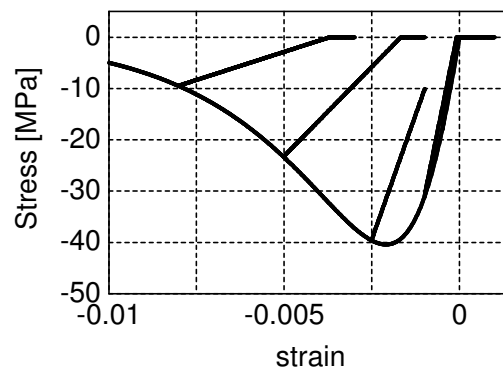


Figure 5: Constitutive Relation of Concrete

Table 1: Material Properties

Concrete		
Beam	Design Strength	$f'_{ck} = 40\text{MPa}$
	Initial Elastic Modulus	$E_c = 31\text{GPa}$
Pier	Design Strength	$f'_{ck} = 27\text{MPa}$
	Initial Elastic Modulus	$E_c = 26.5\text{GPa}$
Reinforcing Bar : SD345		
PC : 12S12.7 / SWPR7B		

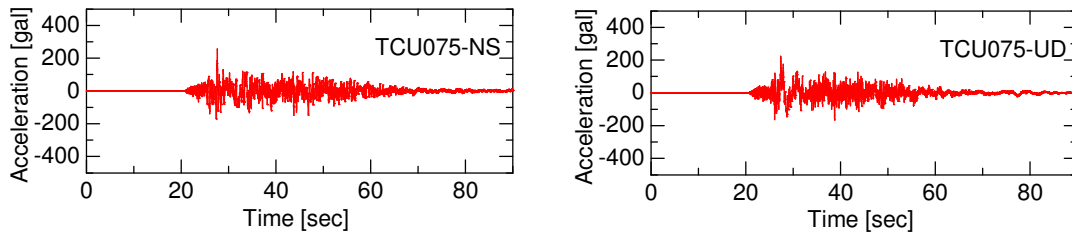
This bridge

Three specimens were prepared to observe the differences of travel time caused by the existence of foreign substance inside concrete, that is,

Slab A : stuffed concrete specimen

#### Time-History of Ground Displacement from Acceleration Record by the EPS Method

In this study, the seismic acceleration records observed in the 921 Chi-Chi earthquake in Taiwan were used. Though there are many observed acceleration records of the quake, this study applied NS and UD components of the acceleration records at TCU075 (Figure 6).



**Figure 6: Ground Acceleration of 921 Chi-Chi Earthquakes at TCU075 in Taiwan (1999)**

Using the EPS method, we can calculate time-history of ground displacement at TCU075 with various residual displacements. Table 2 shows the applied parameters of the EPS method. In the table,  $t_1$  indicates the time when we end the screening the erratic pattern of acceleration less than  $\epsilon_1$  [gal]. Also,  $t_2$  indicates the time when we restart the screening the erratic pattern of acceleration less than  $\epsilon_2$  [gal]. That is, we omit the acceleration less than  $\epsilon_1$  [gal] during the period of  $0 \leq t \leq t_1$  and that less than  $\epsilon_2$  [gal] during the period of  $t_2 \leq t \leq t_f$  (end time of acceleration record).

**Table 2: Parameters of EPS Method**

	$t_1$ [s]	$\epsilon_1$ [gal]	$t_2$ [s]	$\epsilon_2$ [gal]
NS	20.0	0.5	60.0 – 70.0	5.0
UD	20.0	2.0	60.0 – 70.0	20.0

Table 3 shows the residual displacements obtained by the EPS method using various  $t_2$ . Combining the residual displacement, we have various residual relative displacement of the bridge.

The combination of the residual displacement in this study can be found in Table 4. Using the combination, we can represent the normal and reverse slip of from 0.84 to 5.08[m] and we can evaluate the effect of interactions of acceleration and relative displacement.

**Table 3: Residual Displacement of Converted TCU075**

$t_2$ [s]	Residual Disp.		$t_2$ [s]	Residual Disp.		$t_2$ [s]	Residual Disp.	
	NS	UD		NS	UD		NS	UD
60.0	-4.744	-0.565	63.5	+1.191	-0.866	67.0	-0.264	+0.467
60.5	-4.708	+0.256	64.0	+1.762	-0.252	67.5	-0.383	+0.048
61.0	-2.428	-0.269	64.5	+0.247	+0.324	68.0	-0.876	+0.051
61.5	-1.393	-2.211	65.0	-0.415	+1.013	68.5	-0.633	-0.127
62.0	-0.346	-0.869	65.5	-1.701	+1.612	69.0	+0.799	-0.631
62.5	+0.546	-0.828	66.0	-0.965	+0.857	69.5	+1.801	-1.550
63.0	+0.868	-1.412	66.5	-0.115	+0.315	70.0	+1.208	-2.184

## ANALYSIS OF A BRIDGE UNDER BOTH RELATIVE DISPLACEMENT AND INERTIAL FORCE

### Analytical Cases

The dynamic responses under both inertial force and relative displacement can be calculated, by inputting the time-history displacement obtained in chapter 3 to AL/PL and AR/PR in Figure 1. For example, combining the input waves as shown in Figure 7, we have the reverse fault condition with fault angle of 46.4 [degrees] and with fault displacement of 5.08[m].

All the cases of the analyses can be found in Table 4.

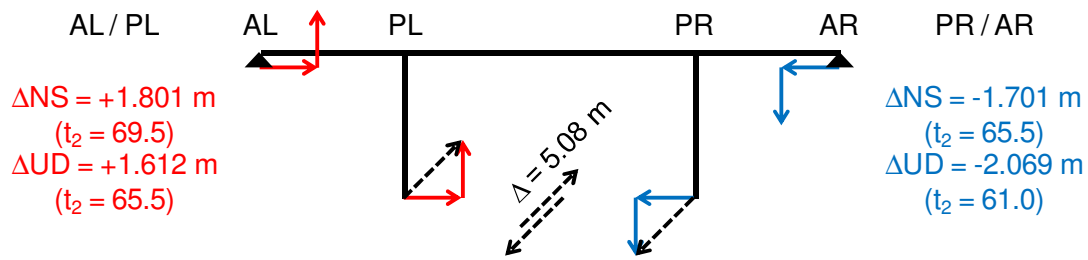


Figure 7: Relation of Combination of Input Displacement Waves and Fault Displacement

Table 4: Analytical Cases

Normal Fault			Reverse Fault		
AL/PL	Fault Disp. and Fault Angle	PR/AR	AL/PL	Fault Disp. and Fault Angle	PR/AR
$\Delta X = +1.208$ ( $t_2 = 70.0s$ ) $\Delta Y = +1.013$ ( $t_2 = 65.0s$ )	NF084 $\Delta = 0.84m$ $\phi = 45.3$	$\Delta X = +1.801$ ( $t_2 = 69.5s$ ) $\Delta Y = +1.612$ ( $t_2 = 65.5s$ )	$\Delta X = +1.801$ ( $t_2 = 69.5s$ ) $\Delta Y = +1.612$ ( $t_2 = 65.5s$ )	RF084 $\Delta = 0.84m$ $\phi = 45.3$	$\Delta X = +1.208$ ( $t_2 = 70.0s$ ) $\Delta Y = +1.013$ ( $t_2 = 65.0s$ )
$\Delta X = +0.799$ ( $t_2 = 69.0s$ ) $\Delta Y = +0.467$ ( $t_2 = 67.0s$ )	NF152 $\Delta = 1.52m$ $\phi = 48.8$			RF152 $\Delta = 1.52m$ $\phi = 48.8$	$\Delta X = +0.799$ ( $t_2 = 69.0s$ ) $\Delta Y = +0.467$ ( $t_2 = 67.0s$ )
$\Delta X = +0.546$ ( $t_2 = 62.5s$ ) $\Delta Y = +0.051$ ( $t_2 = 68.0s$ )	NF200 $\Delta = 2.00m$ $\phi = 51.2$			RF200 $\Delta = 2.00m$ $\phi = 51.2$	$\Delta X = +0.546$ ( $t_2 = 62.5s$ ) $\Delta Y = +0.051$ ( $t_2 = 68.0s$ )
$\Delta X = -0.115$ ( $t_2 = 66.5s$ ) $\Delta Y = -0.127$ ( $t_2 = 68.5s$ )	NF259 $\Delta = 2.59m$ $\phi = 42.2$			RF259 $\Delta = 2.59m$ $\phi = 42.2$	$\Delta X = -0.115$ ( $t_2 = 66.5s$ ) $\Delta Y = -0.127$ ( $t_2 = 68.5s$ )
$\Delta X = -0.264$ ( $t_2 = 67.0s$ ) $\Delta Y = -0.565$ ( $t_2 = 60.0s$ )	NF300 $\Delta = 3.00m$ $\phi = 46.5$			RF300 $\Delta = 3.00m$ $\phi = 46.5$	$\Delta X = -0.264$ ( $t_2 = 67.0s$ ) $\Delta Y = -0.565$ ( $t_2 = 60.0s$ )
$\Delta X = -0.633$ ( $t_2 = 68.5s$ ) $\Delta Y = -0.869$ ( $t_2 = 62.0s$ )	NF348 $\Delta = 3.48m$ $\phi = 45.5$			RF348 $\Delta = 3.48m$ $\phi = 45.5$	$\Delta X = -0.633$ ( $t_2 = 68.5s$ ) $\Delta Y = -0.869$ ( $t_2 = 62.0s$ )
$\Delta X = -0.876$ ( $t_2 = 68.0s$ ) $\Delta Y = -1.412$ ( $t_2 = 63.0s$ )	NF404 $\Delta = 4.04m$ $\phi = 48.5$			RF404 $\Delta = 4.04m$ $\phi = 48.5$	$\Delta X = -0.876$ ( $t_2 = 68.0s$ ) $\Delta Y = -1.412$ ( $t_2 = 63.0s$ )

Using these combinations, dynamic analyses considering both inertial force and relative displacement were achieved. Simultaneously, non-linear static analyses corresponding to each residual displacement were carried out.

#### Analytical Results of Bridge Damage under Normal Fault

Figure 8 shows the analytical results of the bridge damage under normal fault. In the figure, SNF indicates the result of static analysis, and NF indicates the analytical result considering both fault displacement and inertial force.

In addition to this, the circle in the figure means yielding of the element and the square indicates that the element

reached ultimate curvature.

Though no ultimate element appears in SNF084cm, bridge damage obtained by NF084cm shows that the ultimate element appeared at the bottom of right pier.

From (S)NF152 to (S)NF404cm, both analytical results shows that ultimate element appeared on several points. However, the damage of the bridge under both fault displacement with inertial force was severer than that of under only the case considering fault displacement.

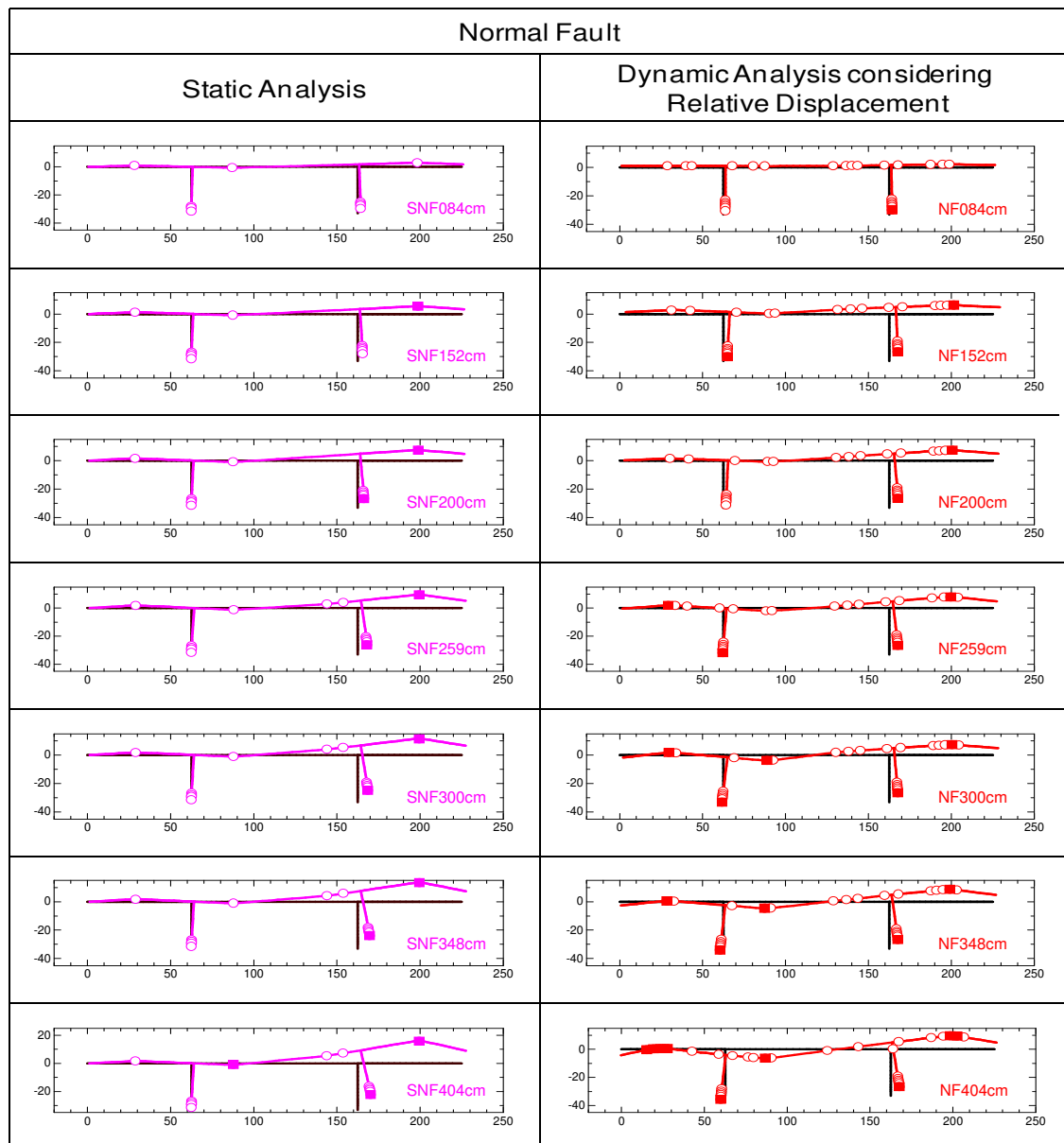


Figure 8: Analytical Results of Bridge Damage under Normal Fault

## Analytical Results of Bridge Damage under Reverse Fault

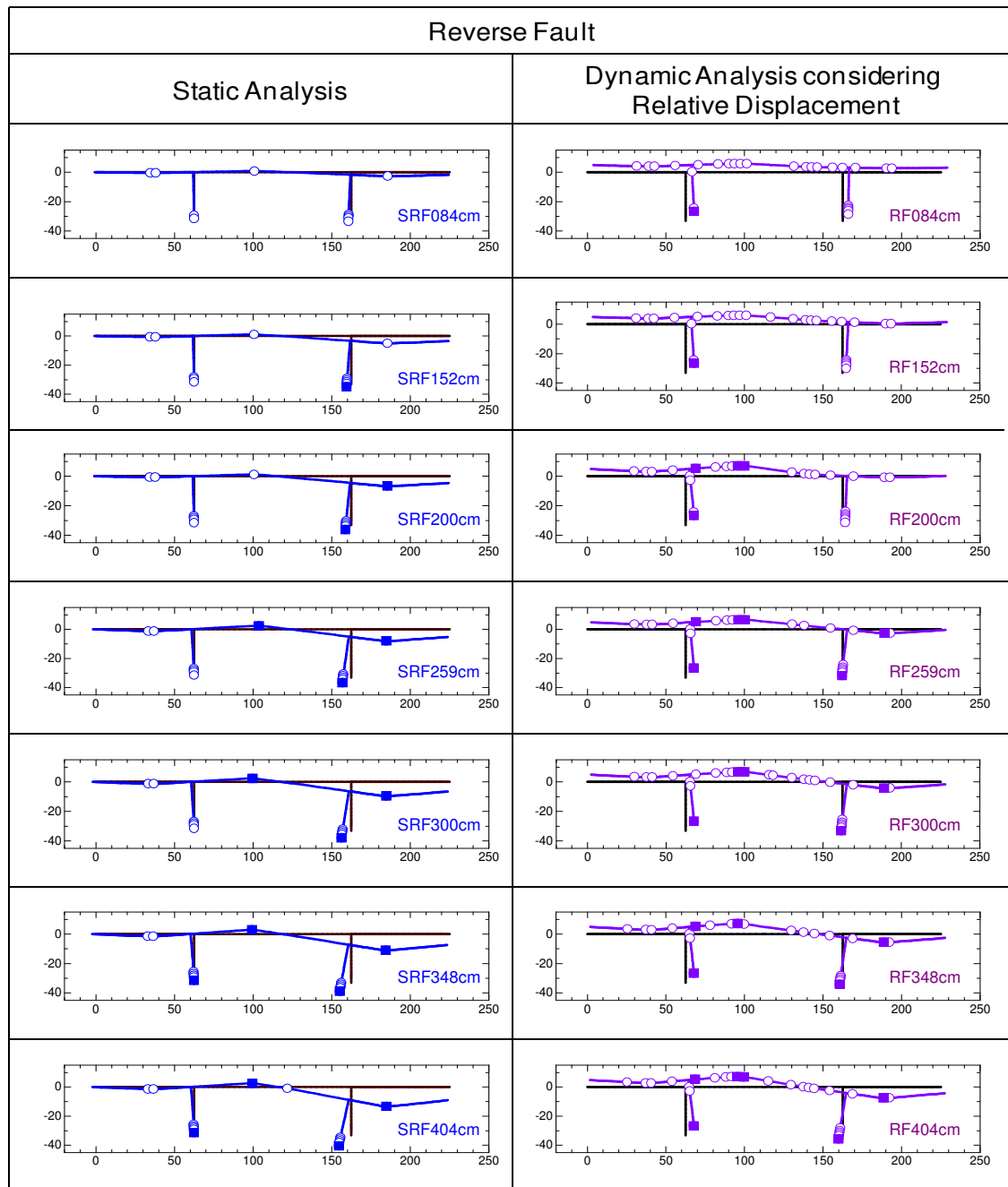


Figure 9: Analytical Result of Bridge Damage under Reverse Fault

Figure 9 shows the analytical result of bridge damage under reverse fault. In the figure, SRF indicates the result of static analysis and RF indicates the analytical result considering both fault displacement and inertial force.

All the tendency of damage distribution is similar to that under normal fault.

It can be seen that, from (S)RF348cm or more relative displacement, the damage distribution resembles each other.

However, the damage distribution of the bridge under both fault displacement with inertial force was severer than that of under only the case considering fault displacement.

## CONCLUSIONS

Some numerical simulations of a rahmen bridge, under normal and reverse fault movement in several fault displacements were carried out in this study. According to the analytical results, it can be concluded as follows.

- In all the cases, the damage distribution of the bridge under fault displacement with inertial force was severer than that of under only the case considering fault displacement.
- There are some cases that we can predict the damage of bridge under fault movement, considering inertial force using static analysis. However, it depends on the fault movement direction.
- The effect of the inertial force to the bridge damage cannot be evaluated by the conventionally static analysis.

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